## LOYOLA COLLEGE (AUTONOMOUS), CHENNAI – 600 034 **B.C.A.** DEGREE EXAMINATION – **COMPUTER APPLICATIONS** SECOND SEMESTER – APRIL 2016 **MT 2101 - MATHEMATICS FOR COMPUTER APPLICATIONS** Date: 26-04-2016 Dept. No. Max.: 100 Marks Time: 01:00-04:00 Part A **Answer ALL questions:** (10X2 = 20)1. Define Skew symmetric matrix and give an example. 2. Find the characteristic equation of $A = \begin{bmatrix} 1 & 2 \\ -3 & 4 \end{bmatrix}$ . 3. If $\alpha$ and $\beta$ are the roots of $2x^2 + 3x + 5 = 0$ , find $\alpha + \beta$ , $\alpha\beta$ . 4. Evaluate $\int_{0}^{\frac{\pi}{2}} \cos^{8}x \, dx$ . 5. Evaluate. $\int \frac{1}{(5x+3)^2} dx$ . 6. Evaluate $\int xe^x dx$ . 7. Find complementary function for $(D^2 + 5D + 6) y = 0$ . 8. Derive the partial differential equation by eliminating the arbitrary constants from z = (x + a)(y + b). 9. Write any two properties of definite integrals. 10. Write the formula for Simpson's $1/3^{rd}$ rule. Part B Answer any FIVE questions: (5 x8 = 40)11. Find the rank of the matrix $A = \begin{bmatrix} 1 & 2 & 3 \\ 3 & 1 & 2 \\ 2 & 3 & 1 \end{bmatrix}$ . 12. Show that $\frac{\sin 6\theta}{\sin \theta} = 32\cos^5 \theta - 32\cos^3 \theta + 6\cos\theta$ . 13. Evaluate $\int_{0}^{1} \int_{0}^{\sqrt{x}} (x+y) dy dx$ . 14. What is the radius of curvature for the curve $x^4 + y^4 = 2$ at the point (1,1). 15. Evaluate $\int \frac{10 dx}{6x^2 - x - 1}$ . 16. Diminish the roots of $2x^5 - x^3 + 10x - 8 = 0$ by 5 and find the transformed equation. 17. Solve xp + qy = z.

18. Given  $z = \sin(3x + 2y) + e^{xy}$  prove that  $\frac{\partial^2 z}{\partial x \partial y} = \frac{\partial^2 z}{\partial y \partial x}$ 

Part C	
Answer any TWO questions:	$(2 \times 20 = 40)$
<b>19.</b> Verify Cayley-Hamilton theorem for the matrix $A = \begin{bmatrix} 1 & 2 & 3 \\ 0 & -1 & 2 \\ 1 & 0 & 2 \end{bmatrix}$ and hence find its invert	se.
	(10+10)
20. a) Evaluate: $\int \frac{x}{(1+x)(x^2+1)} dx$ .	
b) Verify Euler's theorem for the function $u = x^2 + y^2 + 2xy$ .	(15+5)
21. (a) Solve $x^4 - 10x^3 + 26x^2 - 10x + 1 = 0$ . (b) Solve the equation $(D^2 + 6D + 9)y = e^{2x}$ .	(10+10)
	(10+10)
22. (a) Evaluate $\int_{1}^{5} \sqrt{1 + x^2} dx$ using trapezoidal rule with $n = 8$ .	
(b) Use Newton - Raphson method to evaluate $\sqrt{12}$ with the initial condition $x_0 = 3$ correct to four decimal places.	(10+10)

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