LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600034

## B.Sc.DEGREE EXAMINATION - MATHEMATICS

FIFTHSEMESTER - NOVEMBER 2017
MT 5405- FLUID DYNAMICS

Date: 15-11-2017
Dept. No. $\square$ Max. : 100 Marks
Time: 09:00-12:00

## SECTION A

Answer ALL questions:

1. Define stream tube.
2. Show that $q=2 x \vec{i}-y \vec{j}-z \vec{k}$ is a possible motion.
3. The velocity vector q is given by $\vec{q}=\vec{\imath} x-\vec{\jmath} y$ determine the equation of stream line.
4. Write down the boundary condition for the flow when it is moving.
5. What is the complex potential of a source with strength $m$ situated at the points $z=z_{1}$ ?
6. Find the stream function $\psi$, if $\varphi=A\left(x^{2}-y^{2}\right)$ represents a possible fluid motion.
7. Find the vorticity components of a fluid motion, if the velocity components are $u=A y^{2}+B y+C, v=0, w=0$.
8. Define vortex tube and vortex filament.
9. What is lift of an aerofoil?
10. Define camber.

## SECTION B

Answer any FIVE questions:
11. The velocity $\vec{q}$ in a 3-dimensional flow field for an incompressible fluid is $\vec{q}=2 x \dot{i}-y \vec{j}-z \vec{k}$. Determine the equation of streamlines passing through the point $(1,1,1)$.
12. Find the equation of streamlines and path lines of a flow given by $u=\frac{x}{1+t}, v=\frac{y}{1+t}, w=\frac{z}{1+t}$.
13. Draw and explain the working of a Venturi tube.
14. Prove that for the complex potential $\tan ^{-1} z$ the streamlines and equipotentials are circles.
15. Obtain the complex potential due to the image of a doublet with respect to a plane.
16. Show that the velocity vector $\vec{q}$ is every where tangent to the lines in the $X Y$-plane along which $\psi(x, y)=$ a constant.
17. Let $\vec{q}=(A z-B y) \vec{\imath}+(B x-C z) \vec{\jmath}+(C y-A x) \vec{k},(\mathrm{~A}, \mathrm{~B}, \mathrm{C}$ are constants) be the velocity vector of a fluid motion. Find the equation of vortex lines.
18. Discuss the structure of an aerofoil.

## SECTION C

Answer any TWO questions:

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(2 \times 20=40)
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19. (a) Derive the equation of continuity.
(b) If the velocity of an incompressible fluid at the point $(x, y, z)$ is given by $\left(\frac{3 x z}{r^{5}}, \frac{3 y z}{r^{5}}, \frac{3 z^{2}-r^{2}}{r^{5}}\right)$ where $r^{2}=x^{2}+y^{2}+z^{2}$. Prove that the fluid motion is possible and the velocity potential is $\frac{\cos \theta}{r^{2}}$.

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(10+10)
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20. Derive the Euler's equation of motion and deduce the Bernoulli's equation of motion.
21. (a)What arrangement of sources and sinks will give rise to the function $w=\log \left(z-\frac{a^{2}}{z}\right)$ ?
(b)Obtain the complex potential due to the image of a source with respect to a circle.(12+8)
22. (a)Discuss the structure of an aerofoil.
(b)Derive Joukowski transformation.
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