Dept. No. $\square$ Max. : 100 Marks
Time: 01:00-04:00

PART-A
Answer ALL the questions $10 \times 2=20$

1. What is the difference between symmetric and skew symmetric of a matrix?
2. Write the Characteristic equation of $\left[\begin{array}{cc}1 & -2 \\ -5 & 4\end{array}\right]$
3. Define populations and samples.
4. Match each statement in the left-hand column with the correct data set from the right-hand column.
(i). Sample mode is 9
A: $5,7,8,10,13,14$
(ii). Sample mean is 9
B: $1,2,5,9,9,15$
(iii). Sample median is 9
C: $1,2,9,12,12,18$
5. What is complete graph.
6. Give an example for cut vertices?
7. What is Eulerian graph?
8.Define Hamiltonian cycle.
8. Write the formula for Newton- Rapson method to calculate root.
9. Write the Newton's forward difference formula.

## PART-B

## Answer ALL the questions

$5 \times 8=40$
11a) Examine the following equations are consistent or not if so find any one value.
$x+y+z=9, \quad 2 x-y+z=4, \quad 3 x-y+z=6, \quad 4 x-y-2 z=7$
b) Find the rank of the matrix $\mathrm{A}=\left[\begin{array}{cccc}\text { OR } & \\ 1 & 1 & -3 & -1 \\ 4 & -2 & 6 & 8 \\ 15 & -3 & 9 & 21\end{array}\right]$

12 a) Which data value is the sample 90th percentile when the sample size is (i) 8 ,
(ii) 16 , and (iii) 100 ?

## OR

b) The following data give the yearly numbers of law enforcement officers killed in the

United states over 10 years: $164,165,157,164,152,147,148,131,147,155$
Find the sample variance of the number killed in these years.
13 a) Define the following with an example (i) Walk (ii)Path (iii) Trail (iv) Bridges OR
b)i)Prove the following statement. A closed walk of odd length contains a cycle.
ii) Prove the following statement. If $G$ is not connected $\overline{\mathrm{G}}$ bar is connected.

14 a) What is Tree? Draw all trees with 4 and 5 vertices. OR
b) i)Define planar and non-planar.
ii) Prove that $K_{5}$ and $K_{3,3}$ are non-planar.

15a) Find the first approximation of the real root of equation $x^{3}-3 x+1=0$ by regulaFalsi method correct to three places of decimal.

OR
b) Evaluate $\int_{0}^{6} \frac{d x}{1+x^{2}}$ using (i) Simpson's $1 / 3^{\text {rd }}$ rule (ii) Simpson's $3 / 8^{\text {th }}$ rule.

## PART-C

## Answer any TWO

16 a) Verify Cayley Hamilton theorem $\mathrm{A}=\left(\begin{array}{ccc}1 & 0 & 3 \\ 2 & 1 & -1 \\ 1 & -1 & 1\end{array}\right)_{\text {Hence find its inverse }}$
b) Compute the sample correlation coefficient of the data of Table which relates a Person's resting pulse rate to the number of years of school completed.

Table Pulse Rate and Years of School Completed

## Person

|  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ |
| :--- | :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Years of school 12 | 16 | 13 | 18 | 19 | 12 | 18 | 19 | 12 | 14 |  |
| Pulse rate 73 | 67 | 74 | 63 | 73 | 84 | 60 | 62 | 76 | 71 |  |

17 a) Draw the following graphs.
(ii) Simple graph with 5 vertices. (ii) $\mathrm{K}_{5}$. (iii) Regular graph with 5 vertices.
(iv) Planar graph with 5 vertices.(v) Petersen graph
b) Let G be a ( $\mathrm{p}, \mathrm{q}$ ) graph .prove that the following statements are equivalent.
(i) $G$ is a tree
(ii) Every points of G are joined by a unique path.
(iii) G is connected and $\mathrm{p}=\mathrm{q}+1$
(iv) G is acyclic and $\mathrm{p}=\mathrm{q}+1$.
18. a) If $y(10)=35.3, y(15)=32.4, y(20)=29.2, y(25)=26.1, y(30)=23.2, y(35)=20.5$ find $y(12)$ using Newton's forward interpolation formula and
b) Find the Eigen values and Eigen vectors of $\left[\begin{array}{ccc}2 & 2 & 0 \\ 2 & 1 & 1 \\ -7 & 2 & -3\end{array}\right]$
(ii) List some of the properties of the sample correlation coefficient.

