



LOYOLA COLLEGE (AUTONOMOUS), CHENNAI – 600 034

B.Sc. DEGREE EXAMINATION – STATISTICS

THIRD SEMESTER – APRIL 2017

ST 3503 / ST 3500 - STATISTICAL MATHEMATICS - II

Date: 05-05-2017
09:00-12:00

Dept. No.

Max. : 100 Marks

PART-A

Answer ALL the questions:

[10 x 2 =20]

1. Define upper sum of a function on $[a,b]$.
2. Find the MGF of $f(x, \theta) = \theta e^{-\theta x}; x \geq 0$.
3. What do you mean by improper integral?
4. Show that $\int_1^{\infty} \frac{1}{x^2} dx$ is convergent.
5. Define variance-covariance matrix.
6. If X has p.d.f $f(x) = 6x^2, 0 \leq x \leq 1$, find mean of X.
7. Solve the equation $(D^2 - 4D + 13)y$.
8. Define Laplace transform of $f(t)$.
9. When the system of equation is said to be consistent?
10. Determine the Eigen values of the matrix $A = \begin{bmatrix} 5 & 4 \\ 1 & 2 \end{bmatrix}$

PART-B

Answer any Five questions

[5 x 8 = 40]

11. If f and g are Riemann integrable over $[a,b]$, then prove that the sum $f+g$ is also Riemann integrable over $[a,b]$.
12. Evaluate $\iint dx dy$ over the region bounded by $x=0, x=2, y=0, y=2$.
13. Define Gamma integral and obtain its recurrence formulae.
14. Solve the equation $(D^2 + 2D + 1)Y = e^{-x}$.
15. Discuss for all values of λ , the system of equations $x + y + 4z = 6, x + 2y - 2z = 6, \lambda x + y + z = 6$ as regards existence and nature of solutions.
16. Find $L[e^{-3t} \sin^2 t]$
17. Change the order of integration and evaluate $\int_0^3 \int_1^{\sqrt{4-y}} (x+y) dx dy$.
18. Let $f(x) = x^2, 0 \leq x \leq 1$ and let $\sigma_n = \{0, \frac{1}{n}, \frac{2}{n}, \dots, \frac{n-1}{n}, 1\}$. Find $\lim_{n \rightarrow \infty} U[f, \sigma_n]$ and $\lim_{n \rightarrow \infty} L[f, \sigma_n]$.

PART-C

Answer any TWO questions

(2 x 20 = 40]

19. (a) State and prove first fundamental theorem of calculus.

(b) Let f be a bounded function on the closed bounded interval $[a,b]$. Prove that f is Riemann integral iff f is continuous.

[10+10]

20. (a) Discuss the convergence of the following improper integral $\int_0^1 \frac{1}{\sqrt{1-x^2}} dx$

(b) Show that $\int_0^2 x(8-x^3)^{\frac{1}{3}} dx = \frac{8}{3} \beta\left(\frac{2}{3}, \frac{4}{3}\right)$ **[10+10]**

21. (a) Solve $\frac{d^2y}{dx^2} + 4y = 5e^{-x}$, using laplace transform given that $y(0)=2, y'(0)=3$.

(b) Let $f(x, y) = \begin{cases} 8xy & 0 < x < y < 1 \\ 0 & \text{elsewhere} \end{cases}$

Find (a) $E[Y/X=x]$ b) $E[XY/X=x]$ c) $\text{Var}[Y/X=x]$. **[10+10]**

22. (a) State and prove Cayley Hamilton theorem.

(b) Find the characteristic root of the matrix $A = \begin{bmatrix} 1 & 4 \\ 2 & 3 \end{bmatrix}$ and hence find A^{-1} .

[10+10]
