B.Sc. DEGREE EXAMINATION - STATISTICS

SIXTH SEMESTER - NOVEMBER 2016
ST 6607/ST 6604/ST 6601 - OPERATIONS RESEARCH

Date: 15-11-2016
Time: 09:00-12:00
Dept. No. $\square$ Max. : 100 Marks

PART - A
Answer ALL the questions

1. What is linear programming problem?
2. What is a surplus variable?
3. What is the need for artificial variables?
4. What do you mean by decision variables in a LPP?
5. What is a transportation problem?
6. What is an assignment problem?
7. Define the term dummy activity in network analysis.
8. What is Free float?
9. Define saddle point.
10. What is maximin criterion?

> Section - B

Answer Any FIVE questions
11. Give the importance of Operations Research.
12. The ABC manufacturing company can make two products P1 and P2. Each of the product requires time on a cutting machine and a finishing machine. The data is given below:

|  | Product |  | Time available |
| :--- | :---: | :---: | :---: |
|  | P1 | P2 |  |
| Cutting hours (per unit) | 2 | 1 | 8 hrs. |
| Finishing hours (per unit) | 3 | 3 | 12 hrs. |
| Profit (per unit) | Rs. 6 | Rs. 4 |  |
| Maximum sales (unit per week) | - | 200 |  |

Formulate linear programming problem.
13. Explain the Two Phase method.
14. Solve the following unbalanced assignment problem of minimizing total time for doing all jobs.

Jobs

| Operator | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 6 | 2 | 5 | 2 | 6 |
| 2 | 2 | 5 | 8 | 7 | 7 |
| 3 | 7 | 8 | 6 | 9 | 8 |
| 4 | 6 | 2 | 3 | 4 | 5 |
| 5 | 9 | 3 | 8 | 9 | 7 |
| 6 | 4 | 7 | 4 | 6 | 8 |

15. A Project consists of 8 jobs $A$ to $H$ with the following precedence and estimates of time. Draw a project network.

| Job | A | B | C | D | E | F | G | H |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Predecessor | - | - | A, B | A, B | B | D, E | C, F | D, E |
| Time (days) | $\mathbf{1 5}$ | $\mathbf{1 0}$ | $\mathbf{1 0}$ | $\mathbf{1 0}$ | $\mathbf{5}$ | $\mathbf{5}$ | $\mathbf{2 0}$ | $\mathbf{1 0}$ |

16. Explain the time estimates in a PERT network.
17. Using the principle of dominance solve the following game:

| 8 | 10 | 9 | 14 |
| :---: | :---: | :---: | :---: |
| 10 | 11 | 8 | 12 |
| 13 | 12 | 14 | 13 |

18. Solve the game theory problem as a LPP.
Section - C

Answer Any TWO questions
19. (a) Explain the different models of Operations Research. (8 marks)
(b) Solve the following LPP graphically.
(12 marks)

$$
\operatorname{Max} Z=2 X_{1}+3 X_{2}
$$

Subject to $\mathrm{x}_{1}+\mathrm{x}_{2}>=30 ; \mathrm{x}_{2}>=3$; $\mathrm{x}_{2}<=12$;

$$
\begin{aligned}
& x_{1}-x_{2}>=0 ; \quad x_{1}<=20 \\
& x_{1}, x_{2}>=0 .
\end{aligned}
$$

20. (a) Solve the following LPP using Big M method. (12 marks)

Maximize $Z=X_{1}+2 X_{2}$
Subject to $\mathrm{X}_{1}-\mathrm{X}_{2}>=3 ; 2 \mathrm{X}_{1}+\mathrm{X}_{2}<=10$

$$
\mathbf{X}_{1}, \mathrm{X}_{2}>=0 .
$$

(b). Write down the importance of studying primal and dual of LPP. (8 marks)
21. Solve the following transportation problem using Vogels method in order to minimize total transportation cost.
(20 marks)
Destinations

| Origin | D1 | D2 | D3 | D4 | D5 | Availabilities |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 01 | 3 | 5 | 8 | 9 | 11 | 20 |
| 02 | 5 | 4 | 10 | 7 | 10 | 40 |
| 03 | 2 | 5 | 8 | 7 | 5 | 30 |
| Requirements | 10 | 15 | 25 | 30 | 40 | 120 |

22. (a)The following table shows the jobs of a network along with their time estimates.

|  | Duration in days |  |  |
| :---: | :---: | :---: | :---: |
| Job | a | m | b |
| $1-2$ | 2 | 7 | 13 |
| $1-6$ | 2 | 5 | 14 |
| $2-3$ | 2 | 14 | 26 |
| $2-4$ | 7 | 5 | 8 |
| $3-5$ | 5 | 5 | 19 |
| $4-5$ | 3 | 8 | 17 |
| $5-8$ | 8 | 3 | 9 |
| $7-8$ |  | 17 | 32 |

Draw the project network and find the probability that the project is completed in $\mathbf{4 0}$ days.
(b). Solve the following game whose pay-off matrix is

|  |  | Player B |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 |
| Player A | 1 | 4 | -1 | 5 |
|  | 2 | 0 | 5 | 3 |
|  | 3 | 5 | 3 | 7 |

$\qquad$

